




# 4.9 EXERCISES

**HOMEWORK KEY**

-  = WORKED-OUT SOLUTIONS on p. WS9 for Exs. 17, 39, and 73
-  = STANDARDIZED TEST PRACTICE Exs. 2, 44, 45, 68, and 73
-  = MULTIPLE REPRESENTATIONS Ex. 74

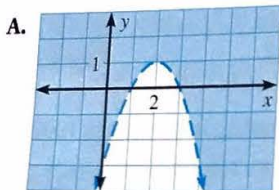
## SKILL PRACTICE

- VOCABULARY** Give an example of a quadratic inequality in one variable and an example of a quadratic inequality in two variables.
- ★ WRITING** Explain how to solve  $x^2 + 6x - 8 < 0$  using a table, by graphing, and algebraically.

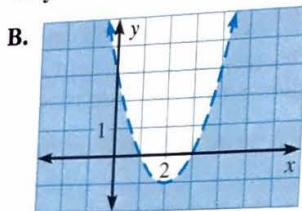
**EXAMPLE 1**  
on p. 300  
for Exs. 3–19

### MATCHING INEQUALITIES WITH GRAPHS Match the inequality with its graph.

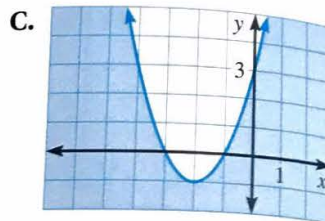
3.  $y \leq x^2 + 4x + 3$



4.  $y > -x^2 + 4x - 3$



5.  $y < x^2 - 4x + 3$

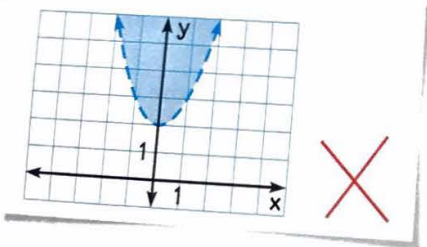


### GRAPHING QUADRATIC INEQUALITIES Graph the inequality.

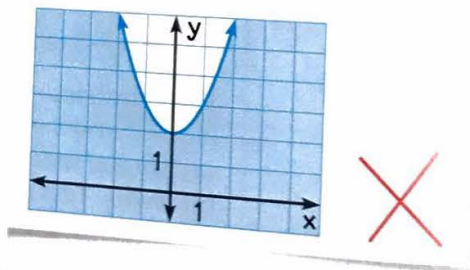
- |                             |                            |                                       |
|-----------------------------|----------------------------|---------------------------------------|
| 6. $y < -x^2$               | 7. $y \geq 4x^2$           | 8. $y > x^2 - 9$                      |
| 9. $y \leq x^2 + 5x$        | 10. $y < x^2 + 4x - 5$     | 11. $y > x^2 + 7x + 12$               |
| 12. $y \leq -x^2 + 3x + 10$ | 13. $y \geq 2x^2 + 5x - 7$ | 14. $y \geq -2x^2 + 9x - 4$           |
| 15. $y < 4x^2 - 3x - 5$     | 16. $y > 0.1x^2 - x + 1.2$ | 17. $y \leq -\frac{2}{3}x^2 + 3x + 1$ |

### ERROR ANALYSIS Describe and correct the error in graphing $y \geq x^2 + 2$ .

18.



19.



### GRAPHING SYSTEMS Graph the system of inequalities.

- |  |   |   |
|--|---|---|
| 20. $y \geq 2x^2$<br>$y < -x^2 + 1$              | 21. $y > -5x^2$<br>$y > 3x^2 - 2$               | 22. $y \geq x^2 - 4$<br>$y \leq -2x^2 + 7x + 4$     |
| 23. $y \leq -x^2 + 4x - 4$<br>$y < 2x^2 + x - 8$ | 24. $y > 3x^2 + 3x - 5$<br>$y < -x^2 + 5x + 10$ | 25. $y \geq x^2 - 3x - 6$<br>$y \geq 2x^2 + 7x + 6$ |

### SOLVING USING A TABLE Solve the inequality using a table.

- |                       |                            |                             |
|-----------------------|----------------------------|-----------------------------|
| 26. $x^2 - 5x < 0$    | 27. $x^2 + 2x - 3 > 0$     | 28. $x^2 + 3x \leq 10$      |
| 29. $x^2 - 2x \geq 8$ | 30. $-x^2 + 15x - 50 > 0$  | 31. $x^2 - 10x < -16$       |
| 32. $x^2 - 4x > 12$   | 33. $3x^2 - 6x - 2 \leq 7$ | 34. $2x^2 - 6x - 9 \geq 11$ |

EXAMPLE 5  
p. 302  
Exs. 35-43

**SOLVING BY GRAPHING** Solve the inequality by graphing.

35.  $x^2 - 6x < 0$   
 36.  $x^2 + 8x \leq -7$   
 37.  $x^2 - 4x + 2 > 0$   
 38.  $x^2 + 6x + 3 > 0$   
 39.  $3x^2 + 2x - 8 \leq 0$   
 40.  $3x^2 + 5x - 3 < 1$   
 41.  $-6x^2 + 19x \geq 10$   
 42.  $-\frac{1}{2}x^2 + 4x \geq 1$   
 43.  $4x^2 - 10x - 7 < 10$

44. **★ MULTIPLE CHOICE** What is the solution of  $3x^2 - x - 4 > 0$ ?  
 (A)  $x < -1$  or  $x > \frac{4}{3}$   
 (B)  $-1 < x < \frac{4}{3}$   
 (C)  $x < -\frac{4}{3}$  or  $x > 1$   
 (D)  $1 < x < \frac{4}{3}$
45. **★ MULTIPLE CHOICE** What is the solution of  $2x^2 + 9x \leq 56$ ?  
 (A)  $x \leq -8$  or  $x \geq 3.5$   
 (B)  $-8 \leq x \leq 3.5$   
 (C)  $x \leq 0$  or  $x \geq 4.5$   
 (D)  $0 \leq x \leq 4.5$

**SOLVING ALGEBRAICALLY** Solve the inequality algebraically.

46.  $4x^2 < 25$   
 47.  $x^2 + 10x + 9 < 0$   
 48.  $x^2 - 11x \geq -28$   
 49.  $3x^2 - 13x > 10$   
 50.  $2x^2 - 5x - 3 \leq 0$   
 51.  $4x^2 + 8x - 21 \geq 0$   
 52.  $-4x^2 - x + 3 \leq 0$   
 53.  $5x^2 - 6x - 2 \leq 0$   
 54.  $-3x^2 + 10x > -2$   
 55.  $-2x^2 - 7x \geq 4$   
 56.  $3x^2 + 1 < 15x$   
 57.  $6x^2 - 5 > 8x$

58. **GRAPHING CALCULATOR** In this exercise, you will use a different graphical method to solve Example 6 on page 303.

- a. Enter the equations  $y = 7.51x^2 - 16.4x + 35.0$  and  $y = 100$  into a graphing calculator.  
 b. Graph the equations from part (a) for  $0 \leq x \leq 9$  and  $0 \leq y \leq 300$ .  
 c. Use the *intersect* feature to find the point where the graphs intersect.  
 d. During what years was the number of participating teams greater than 100? *Explain* your reasoning.

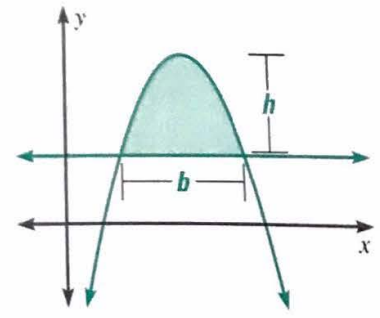
**CHOOSING A METHOD** Solve the inequality using any method.

59.  $8x^2 - 3x + 1 < 10$   
 60.  $4x^2 + 11x + 3 \geq -3$   
 61.  $-x^2 - 2x - 1 > 2$   
 62.  $-3x^2 + 4x - 5 \leq 2$   
 63.  $x^2 - 7x + 4 > 5x - 2$   
 64.  $2x^2 + 9x - 1 \geq -3x + 1$   
 65.  $3x^2 - 2x + 1 \leq -x^2 + 1$   
 66.  $5x^2 + x - 7 < 3x^2 - 4x$   
 67.  $6x^2 - 5x + 2 < -3x^2 + x$

68. **★ OPEN-ENDED MATH** Write a quadratic inequality in one variable that has a solution of  $x < -2$  or  $x > 5$ .

69. **CHALLENGE** The area  $A$  of the region bounded by a parabola and a horizontal line is given by  $A = \frac{2}{3}bh$  where  $b$  and  $h$  are as defined in the diagram. Find the area of the region determined by each pair of inequalities.

- a.  $y \leq -x^2 + 4x$   
 $y \geq 0$   
 b.  $y \geq x^2 - 4x - 5$   
 $y \leq 3$



## PROBLEM SOLVING

### EXAMPLE 2

on p. 301  
for Exs. 70–71

70. **ENGINEERING** A wire rope can safely support a weight  $W$  (in pounds) provided  $W \leq 8000d^2$  where  $d$  is the rope's diameter (in inches). Graph the inequality.

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71. **WOODWORKING** A hardwood shelf in a wooden bookcase can safely support a weight  $W$  (in pounds) provided  $W \leq 115x^2$  where  $x$  is the shelf's thickness (in inches). Graph the inequality.

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### EXAMPLE 6

on p. 303  
for Exs. 72–74

72. **ARCHITECTURE** The arch of the Sydney Harbor Bridge in Sydney, Australia, can be modeled by  $y = -0.00211x^2 + 1.06x$  where  $x$  is the distance (in meters) from the left pylons and  $y$  is the height (in meters) of the arch above the water. For what distances  $x$  is the arch above the road?



73. **★ SHORT RESPONSE** The length  $L$  (in millimeters) of the larvae of the black porgy fish can be modeled by

$$L(x) = 0.00170x^2 + 0.145x + 2.35, \quad 0 \leq x \leq 40$$

where  $x$  is the age (in days) of the larvae. Write and solve an inequality to find at what ages a larvae's length tends to be greater than 10 millimeters. *Explain* how the given domain affects the solution.

74. **◆ MULTIPLE REPRESENTATIONS** A study found that a driver's reaction time  $A(x)$  to audio stimuli and his or her reaction time  $V(x)$  to visual stimuli (both in milliseconds) can be modeled by

$$A(x) = 0.0051x^2 - 0.319x + 15, \quad 16 \leq x \leq 70$$

$$V(x) = 0.005x^2 - 0.23x + 22, \quad 16 \leq x \leq 70$$

where  $x$  is the driver's age (in years).

- Writing an Inequality** Write an inequality that you can use to find the  $x$ -values for which  $A(x)$  is less than  $V(x)$ .
- Making a Table** Use a table to find the solution of the inequality from part (a). Your table should contain  $x$ -values from 16 to 70 in increments of 6.
- Drawing a Graph** Check the solution you found in part (b) by using a graphing calculator to solve the inequality  $A(x) < V(x)$  graphically. *Describe* how you used the domain  $16 \leq x \leq 70$  to determine a reasonable solution.
- Interpret** Based on your results from parts (b) and (c), do you think a driver would react more quickly to a traffic light changing from green to yellow or to the siren of an approaching ambulance? *Explain*.

**○ = WORKED-OUT SOLUTIONS**  
on p. WS1

**★ = STANDARDIZED**  
**TEST PRACTICE**

**◆ = MULTIPLE**  
**REPRESENTATIONS**

75. **SOCCER** The path of a soccer ball kicked from the ground can be modeled by

$$y = -0.0540x^2 + 1.43x$$

where  $x$  is the horizontal distance (in feet) from where the ball was kicked and  $y$  is the corresponding height (in feet).

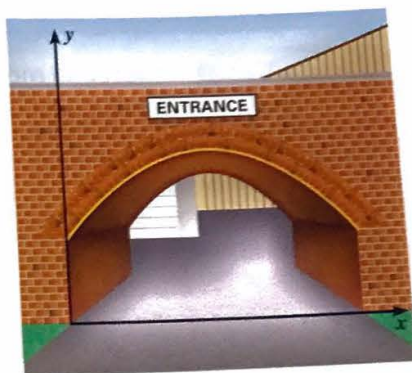
- A soccer goal is 8 feet high. Write and solve an inequality to find at what values of  $x$  the ball is low enough to go into the goal.
- A soccer player kicks the ball toward the goal from a distance of 15 feet away. No one is blocking the goal. Will the player score a goal? Explain your reasoning.

76. **MULTI-STEP PROBLEM** A truck that is 11 feet tall and 7 feet wide is traveling under an arch. The arch can be modeled by

$$y = -0.0625x^2 + 1.25x + 5.75$$

where  $x$  and  $y$  are measured in feet.

- Will the truck fit under the arch? Explain your reasoning.
- What is the maximum width that a truck 11 feet tall can have and still make it under the arch?
- What is the maximum height that a truck 7 feet wide can have and still make it under the arch?



77. **CHALLENGE** For clear blue ice on lakes and ponds, the maximum weight  $w$  (in tons) that the ice can support is given by

$$w(x) = 0.1x^2 - 0.5x - 5$$

where  $x$  is the thickness of the ice (in inches).

- Calculate** What thicknesses of ice can support a weight of 20 tons?
- Interpret** Explain how you can use the graph of  $w(x)$  to determine the minimum  $x$ -value in the domain for which the function gives meaningful results.



## MISSOURI MIXED REVIEW

TEST PRACTICE at classzone.com

78. Rachel is a cross-country runner. Her coach recorded the data shown at the right during a timed practice run. If Rachel continues to run at the same rate, what is the approximate distance she will run in 25 minutes?

Time (minutes)	Distance (kilometers)
6	1.2
12	2.4
15	3

- 4.2 km
- 5 km
- 6 km
- 10 km

79. Which set of dimensions corresponds to a pyramid similar to the one shown?

- $w = 1$  unit,  $l = 2$  units,  $h = 4$  units
- $w = 2$  units,  $l = 3$  units,  $h = 6$  units
- $w = 3$  units,  $l = 4$  units,  $h = 8$  units
- $w = 4$  units,  $l = 6$  units,  $h = 12$  units

